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CONFERENCE PROCEEDINGS • Volume 13

CATEGORY THEORY 1991

Proceedings of an
International Summer Category Theory Meeting
held June 23–30, 1991

R. A. G. Seely, Editor

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Preface

This volume is the published proceedings of the 1991 International Summer Category Theory Meeting (*Category Theory 1991*), which was held in Montréal, Canada during the week of June 23–30. As category theory approaches its first half-century it is clear that it continues to grow, finding new applications in domains that would have seemed inconceivable a generation ago, as well as in its traditional contexts. Some of this diversity is reflected in the papers in this volume.

The conference would not have been possible without the efforts of M. Barr, T. Fox, Raffaella Bruno, Monique Lemire, and the Scientific committee: Jim Lambek, M. Makkai, Andy Pitts, Gonzalo Reyes, Myles Tierney, and Richard Wood. In the production of this book I have been helped by the fine work (and especially the promptness) of the anonymous referees, of the authors themselves, and by Michael Barr, whose support was invaluable. The meeting was partially supported by grants from Le Fonds FCAR, Québec.

R. A. G. Seely



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