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TITLE:

CONVENTIONS FOR QUANTUM PSEUDOCODE

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Conventions for Quantum Pseudocode

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Abstract

A few conventions for thinking about and writing quantum pseudocode are proposed. The conventions can be used for presenting any quantum algorithm down to the lowest level and are consistent with a quantum random access machine (QRAM) model for quantum computing. In principle a formal version of quantum pseudocode could be used in a future extension of a conventional language.

Note: This report is preliminary. Please let me know of any suggestions, omissions or errors so that I can correct them before distributing this work more widely.

1 Introduction

It is increasingly clear that practical quantum computing will take place on a classical machine with access to quantum registers. The classical machine performs off-line classical computations and controls the evolution of the quantum registers by initializing them in certain preparable states, operating on them with elementary unitary operations and measuring them when needed. Although architectures for an integrated machine are far from established, a suitable model for describing algorithms of this mixed nature is that of the quantum random access machine (QRAM). A quantum random access machine is a random access machine in the traditional sense with the ability to perform a restricted set of operations on quantum registers. These operations consist of state preparation, some unitary operations

and measurement¹. A QRAM can implement any local quantum algorithm starting from classical states. Some situations require operating on quantum registers in states prepared by another source (for example a quantum channel, or a quantum transmission overheard by an eavesdropper), in which case the QRAM is given access to the required state in registers prepared elsewhere.

In classical computing, algorithms are often described using a loosely defined convention for writing pseudocode. Good pseudocode is based on computational primitives easily implemented in most computational systems and has familiar semantics. In principle, implementing pseudocode on a real computer should require little effort. In practice, pseudocode does not provide sufficiently detailed implementations of the required data structures and often relies on fairly high-level mathematical expressions, unbounded integers and arbitrary accuracy real numbers. However, a good convention for writing pseudocode is an indispensible tool for describing and formally analyzing algorithms and data structures.

Conventions for writing quantum pseudocode have not yet been established. In fact, most quantum algorithms are described using a mixture of quantum circuits, classical algorithms and mathematical description. Exceptions include algorithms described in [2, 5]. The purpose of this report is to provide some suggestions for unifying these methods in a familiar framework. The suggestions include methods for handling quantum registers in pseudocode by introducing notation for distinguishing quantum from classical registers, annotation for specifying the extent of entanglement of quantum registers and methods for initializing, using and measuring quantum registers. On a higher level, there are several meta-operations that have proved useful in quantum computation. These include reversing a quantum operation not involving a measurement, conditioning of quantum operations and converting a classical algorithm to a reversible one. In this report the meta-operations are described informally. Systematic implementations of these algorithms will be given elsewhere.

The suggestions for writing quantum pseudocode are still incomplete. The extent to which classical and quantum registers should be separated and annotated remains to be seen. The most useful meta-operations need to be better formalized in conjunction with a more formal treatment of the syntax and the semantics of quantum pseudocode. Conventions are likely to change as experience in writing quantum algorithms is gained. Future

¹It may be convenient to allow application of general superoperators. However any superoperator can be simulated by unitary operations and measurement.

versions of this report will reflect such changes and include more examples.

2 Quantum Pseudocode

2.1 Quantum and Classical Registers

Quantum pseudocode is an extension of conventional pseudocode such as described in [7]. The most important aspect of the extension concerns the introduction and use of quantum registers. We take the view that a quantum register is just a classical register not known to be in a classical state. The basic difference between a classical and a quantum register is that the latter can be in a superposition of the available classical states and allows only a restricted set of operations. Except for the restriction on operations, the distinction is primarily semantic. If a register is known to be classical, all the usual operations familiar from traditional programming can be applied to it. It is therefore convenient to explicitly annotate those registers which may be in superpositions and potentially entangled with other quantum registers.

The state of a machine executing quantum pseudocode can be described by the contents of the classical registers and other classical structures (such as program counters) required for the basic architecture, together with a complex superposition of the classical states of those registers that have been declared (explicitly or implicitly) as quantum. An operation on any quantum register may have an effect on the total superposition involving the other quantum registers. Thus there are (with some exceptions) no side-effect free operations on a quantum register. However, it may be convenient to explicitly partition the quantum registers into sets known to be in independent (that is factorizable) states. Two parts must be merged whenever a unitary operation is applied involving both of them. They can be separated if it can be proven that the operations result in a factorizable state under all circumstances.

2.2 Methods for Introducing a Quantum Register

The simplest method for introducing a quantum register is to do it implicitly, by applying a proper unitary operation to a classical register or by calling a subroutine which returns a quantum state. Quantum registers can be

²An operation on a quantum register will not affect the density matrix induced on the others. However, the phases and the entanglement are modified, which can affect the outcome of future operations.

distinguished by underlines³. The following fragment of code gives examples:

QIntroExamples()

 $a \leftarrow 0^{5}$

C: Initializes a classical register a to contain 5 bits in the 0 state.

 $a \leftarrow a$

C: This converts a to a quantum register without applying any operations. Future operations involving \underline{a} are restricted to quantum operations.

 $d \leftarrow 10$

C: d is declared a classical register containing the integer

 $\underline{b} \leftarrow \text{UniformSuperposition}(d)$

C: UniformSuperposition(d) takes a classical input (in this case an integer) and introduces a new quantum register in an initial state. Its state is independent of any other quantum register in the system.

 $\underline{c} \leftarrow \text{MULTIPLY}(\underline{b}, d)$

C: Here a subroutine takes both quantum and classical input. A new quantum register \underline{c} is introduced, which may be entangled with \underline{b} .

 $x \leftarrow \text{DoSomethingClassical}()$

 $\underline{x} \leftarrow \text{DoSomethingQuantum}(x, d)$

C: The fact that x is converted and/or involved in quantum operation in the subroutine is made explicit by the assignment statement with the quantum annotation on the left.

The conventions used here require that a register symbol is always considered either classical or quantum. Semantically, which is in effect depends on the most recent operation applied to it. If it has been declared as quantum, or a proper quantum operation has been applied, then no further classical operations can be used until it is measured. The syntactic annota-

³Another option might be to use the notation $|a\rangle$ to indicate that register a is participating in the quantum state of the system. However, this is not quite consistent with the practice of using $|x\rangle$ to denote the state labelled x.

tion helps keep track of the semantics of a register in any given section of code. Correctness of the annotation may require online consistency checking, though code where the annotation is not obviously correct for syntactic reasons should be avoided. Some of these issues can be avoided by using each register in only one mode, either classical or quantum. This convention is used in [5], where capitals are used to distinguish quantum registers from classical ones. Note that if registers which may be in a proper superposition are consistently annotated, then the issue of whether classical registers are disjoint from quantum ones is primarily a semantic issue. In either case, annotation can be used to indicate available knowledge on the nature of the superposition in a register, e.g. whether the state of the register is purely classical or not.

As can be seen from the code above, the idea is to use assignment with quantum annotation on the left to indicate the introduction of quantum registers or the conversion of classical registers to quantum registers by subroutines or other operations. Thus assignments with a quantum register on the left always have the property that the register did not previously exist or is a classical argument on the right. Further rules for assignments involving multiple types of registers will be given when measurement is introduced. Although we have not done so here, it may be desirable to distinguish such generalized assignments from classical assignments by use of a different left arrow.

2.3 Applying Unitary Operators to Quantum Registers

Operations on quantum registers are restricted to unitary operators and measurement. Measurement is discussed in the next section. Some additional meta-operations will be given later. Unitary operators can only be applied to classical registers in a suitable conversion statement, such as those introduced in the previous paragraphs. Which unitary operators are applied can be controlled by the contents of classical registers using the usual conditionals. Thus unitary operations can be implicit in subroutine calls with both classical and quantum arguments. What unitary operations are accessible must be specified. In principle, any algorithm can be refined to one and two qubit unitary operators [1]. If the algorithm is generic, any sufficiently powerful set may be chosen and the task of reducing the algorithm to the device level can be left to the implementer. For efficiency purposes it might be worth specifying an algorithm directly in terms of the most elementary operations available in a given device, such as laser pulses for an ion trap computer [4].

If it is necessary to refine an algorithm to the qubit level, then it is useful to have notation for extracting a (qu)bit from a register of a given declared length. Indices are used for this purpose. As an illustration we give pseudocode of a full quantum implementation of the Fourier transform mod 2^d .

Define the Hadamard operation on one qubit as

$$\mathcal{H}(\underline{a}) = \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \underline{a},$$

The phase shift of $|1\rangle$ by ϕ is given by

$$\mathcal{R}_{\phi}(\underline{a}) = \left(egin{array}{cc} 1 & 0 \ 0 & e^{i\phi} \end{array}
ight)\underline{a}\,.$$

The controlled phase shift of \underline{b} , controlled by $|1\rangle$ of \underline{a} , is denoted by

if
$$\underline{a}$$
 then $\mathcal{R}_{\phi}(\underline{b})$.

See below for more information on quantum conditionals.

FOURIER(\underline{a}, d)

Input: A quantum register \underline{a} with d qubits. The most significant qubit has index d-1.

Output: The amplitudes of \underline{a} are Fourier transformed over \mathbb{Z}_{2^d} . The most significant bit in the output has index 0, that is the ordering is reversed.

$$\begin{aligned} \omega &\leftarrow e^{i2\pi/2^d} \\ \text{for } i = d-1 \text{ to } i = 0 \\ \text{for } j = d-1 \text{ to } j = i+1 \\ & \underline{\text{if }} \underline{a_j} \underline{\text{then }} \mathcal{R}_{\omega^{2^{d-i-1}+j}}(\underline{a_i}) \\ & \overline{\text{C:}} \end{aligned} \text{ If the phase change in this unitary operation is much smaller than then } 1/n^2, \text{ the operation can be omitted at a correspondingly small cost in the accuracy of the final state [6]. Thus this procedure can be modified to accept a precision parameter to reduce the number of quantum operations required.} \end{aligned}$$

 $\mathcal{H}(a_i)$

The pseudocode makes liberal use of integer and real registers which are not explicitly represented at the bit level. The data type of a register is implicit in the first assignment statement which introduces it.

2.4 Measuring a Quantum Register

The most common method for returning a quantum register to a classical state is to measure it. The assignment statement $a \leftarrow \underline{a}$ can be used to indicate the measurement. The outcome of this operation is inherently random and has side effects on the quantum state of the part of the system previously entangled with \underline{a} . If a quantum input of a subroutine is measured in the subroutine without being reintroduced as a quantum register, this can be indicated by an assignment statement:

$a \leftarrow \text{DoAndMeasure}(\underline{a}, \underline{b}, c)$.

The most general assignment statement can have multiple registers appearing on the left. The rules are as follows:

- (i) No register can appear in its quantum form on both sides.
- (ii) A register appearing only on the left must either be classical (in which case the original contents are lost), or not previously declared.
- (iii) A register appearing only on the right can experience side effects during the operation. That is registers, in particular quantum registers, are assumed to be passed by reference. It is a good idea to specify what side effects are experienced by argument registers in the description of the output of the subroutine.
- (iv) A register appearing in its quantum form on the right and the classical form on the left is measured during the operation, either explicitly, or implicitly at the end.

For the purpose of clarity it is a good idea to indicate all transitions between classical and quantum by use of the generalized assignment statement.

As an example of the use of measurement for obtaining a more efficient implementation, here is pseudocode for the measured Fourier transform described in [8].

$a \leftarrow \text{MeasuredFourier}(\underline{a}, d)$

Input: A quantum register \underline{a} with d qubits. The most significant qubit has index d-1.

Output: The amplitudes of \underline{a} are Fourier transformed over \mathbb{Z}_{2^d} , and then measured. The most significant bit in the output has index 0, that is the ordering is reversed. The input quantum register is returned to a classical state in the process.

```
\omega \leftarrow e^{i2\pi/2^d}
\phi \leftarrow 0
for i = d - 1 to i = 0
\mathcal{R}_{\phi}(\underline{a_i})
\mathcal{H}(\underline{a_i})
a_i \leftarrow \underline{a_i}
\phi \leftarrow (\phi + a_i\pi)/2
```

C: The expression on the right of this assignment statement requires a_i to be in a classical state as it involves operations not allowed for quantum registers.

2.5 Annotation of Quantum Registers

As mentioned previously, it may sometimes be convenient to explicitly annotate registers participating in independent quantum states. There is no convention for this at the moment. Suggestions include modifying the underline which indicates a quantum register and various versions of pre-, super-, and subscripts.

2.6 Quantum Pseudocode without Annotation

In principle, one can write quantum pseudocode without using annotation. Note that only registers declared as bit sequences can be used for quantum operations⁴. From an operational point of view it suffices to describe what happens to a register which is currently in superposition when subjected to a classical (non-reversible) operation. The simplest solution is to automatically force a measurement in that case and have the classical operator act on the result. This includes assignment operations to previously declared registers. An assignment operation involving a new quantum register introduced by the subroutine replaces the target register completely. Any quantum information is considered lost. The operation is equivalent to a measurement with the outcome discarded (dissipation of the contents). An assignment operation of a quantum to a classical register is a method for measuring the quantum register and accessing the result elsewhere.

As can be seen, quantum pseudocode without annotation makes sense operationally. However, correct annotation is helpful for understanding and

⁴This may change as more sophisticated quantum data structures are developed.

analyzing an algorithm. It also helps the systematic application of some of the meta-operations that are described next.

2.7 Reversing a Quantum Subroutine

One of the meta-operations frequently used in describing quantum algorithms is reversal. This operation is usually introduced for reversibly returning temporary registers to their starting state and for reducing quantum register usage in converting a classical algorithm to a reversible one (see [3, 9, 2] for discussions and examples).

A subroutine which performs quantum operations can be reversed provided it does not contain measurement operations. To perform the reversal, the classical component of the subroutine must be implemented in a way which explicitly keeps track of all unitary operators applied to quantum registers. A simple method for doing this is to first run the subroutine forward without actually applying any of the unitary operators, and then applying the inverses of the unitary operators in reverse. In order to avoid ambiguities, the forward subroutine must have no side effects on classical input registers and no classical output.

The simplest case involves reversing a unitary operation. For example, reverse $\mathcal{H}(\underline{a})$ applies the inverse of the Hadamard transform to qubit \underline{a} (this happens to be the same operation). For a less trivial example, consider the subroutine

$$\underline{b} \leftarrow \text{Add}(\underline{a}, c)$$
,

which adds the contents of the classical register c to \underline{a} and places the result coherently into \underline{b} . The operation

reverse
$$\underline{b} \leftarrow \text{Add}(\underline{a}, c)$$

applies the inverses of quantum operations that would be executed by the given subroutine in reverse order. Thus the code

REVERSINGEXAMPLE()

$$\underline{a}, \underline{x}, c \leftarrow \text{Initialize()}$$
 $\underline{b} \leftarrow \text{Add}(\underline{a}, c)$
 $\underline{\text{if } b_0 \text{ then }} \text{DoStuffTo}(\underline{x})$
 $\text{reverse } \underline{b} \leftarrow \text{Add}(\underline{a}, c)$

returns \underline{b} to whatever classical state it started in when it was introduced

in the first call to ADD(). This does not normally hold if ADD() is replaced by an arbitrary quantum operation or if the reverse of ADD() is applied to a general input state. In these cases \underline{b} may end up in an entangled superposition.

2.8 Quantum Registers in Provably Classical States

In implementing quantum subroutines, it is often the case that temporary quantum registers are introduced in such a way that at the end (or at various other stages) they are known to have returned to a classical state, at least if the operations are applied perfectly. This often happens when transforming a classical algorithm into a reversible form which is to be applied coherently to a quantum input (see below). It is useful to be able to assert this fact (with proof if not obvious) and explicitly return the register to the classical form without an actual measurement. (A measurement might make the subroutine apparently non-reversible.) The following (useless) fragment of code gives an example. Let c-not(a,b,) be the controlled-not operation, controlled by the first argument. Note that this is a classical reversible operation and can therefore be used in both classical and quantum contexts.

IsCLASSICALEXAMPLE()

```
\underline{a} \leftarrow \text{GENERATE}()
\underline{b} \leftarrow 0
\underline{b} \leftarrow \text{c-not}(\underline{a}, b,)
\underline{c} \leftarrow \text{c-not}(\underline{b}, c,)
reverse \underline{b} \leftarrow \text{c-not}(\underline{a}, \underline{b},)
C: This is the same as <math>\underline{b} \leftarrow \text{c-not}(\underline{a}, \underline{b},)
\underline{b} \leftarrow \text{isClassical } \underline{b}
Proof. By checking on the classical states.
```

In cases where a register \underline{b} is provably in a classical state, the contents are determined by the classical information in the computation. Usually, as in the example above, the contents are simply returned to a known initial state. In either case, the register can be used again without affecting reversibility of the code.

Another method for reusing a quantum register while maintaining our ability to formally reverse a subroutine is to let its state dissipate. This means that the contents of the register are no longer needed, but also that

any coherent information in it is lost with possible side effects on the remaining quantum state. To dissipate and re-initalize \underline{b} one can use the statement $b \leftarrow 0$ after dissipating \underline{b} . Simply stating $b \leftarrow 0$ in principle accomplishes the same thing (see the section on annotation free pseudocode), but is not explicit about the conversion of the quantum register. The important property of such an operation is that the contents of the register have no effect on future computations. The effect of reversing a subroutine with such dissipation events but no measurements is still predictable (the sequence of unitary operations applied can only depend on the classical input, not on the quantum input), but not equivalent to the inverse operation. In effect unitary operations involving the environment have occured and these operations are not reversed when applying the inverse sequence of unitary operators. So far, allowing the contents of a register to dissipate appears to be useful only if it is known to have returned to a classical state already. Exceptions might be found in potential applications to quantum non-deterministic computing [10].

2.9 Conditioning a Quantum Subroutine

A frequently used technique, for example in reversible implementations of classical functions, is to condition the application of a sequence of unitary (or classical reversible) operations on the state of a controlling qubit. Provided that a subroutine is side effect free on the classical input, has no classical output and avoids measurement and dissipation, it can be conditioned by applying each of its unitary operations if the controlling qubit is in $|1\rangle$ or applying the identity if it is in $|0\rangle$. The overall effect is that of a unitary operation involving the controlling qubit. We can use a version of the traditional if-then statement to perform quantum conditioning. For example

implement a controlled-not and a Toffoli gate, respectively.

Multiple conditionings can be efficiently implemented by the use of an *enable* qubit [2]. An enable qubit is an auxiliary qubit which is introduced specifically for controlling the quantum operations in a subroutine.

2.10 Making a Classical Function Reversible

For most of the interesting quantum algorithms to date, an important component is to entangle a quantum register with the output of a function. This is an operation of the form $|a\rangle|0\rangle \rightarrow |a\rangle|f(a)\rangle$, where a classical algorithm for the function is known. The classical algorithm cannot be applied directly because it usually involves many non-reversible operations. Techniques for systematically converting non-reversible algorithms into reversible ones are known [3], but usually do not yield the most space efficient implementation. However, if complexity is not a major issue in describing an algorithm, one can use a meta-operation on a classically implemented function to indicate a reversible implementation. If $b \leftarrow \text{FUNCTION}(a)$ is given in a classical implementation without side effects on a or other classical inputs, then $\underline{b} \leftarrow \text{FUNCTION}^{R}(\underline{a})$ is interpreted as a reversible implementation with the desired effect and all ancilla quantum registers reversibly returned to their initial states.

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A few conventions for thinking about and writing quantum pseudocode are proposed. The conventions can be used for presenting any quantum algorithm down to the lowest level and are consistent with a quantum random access machine (QRAM) model for quantum computing. In principle a formal version of quantum pseudocode could be used in a future extension of a conventional language.

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