

# A space-time resolved view of the Schwinger effect

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# Motivation: An artist's view

**Boom! From Light Comes Matter**



[Gil Eisner]

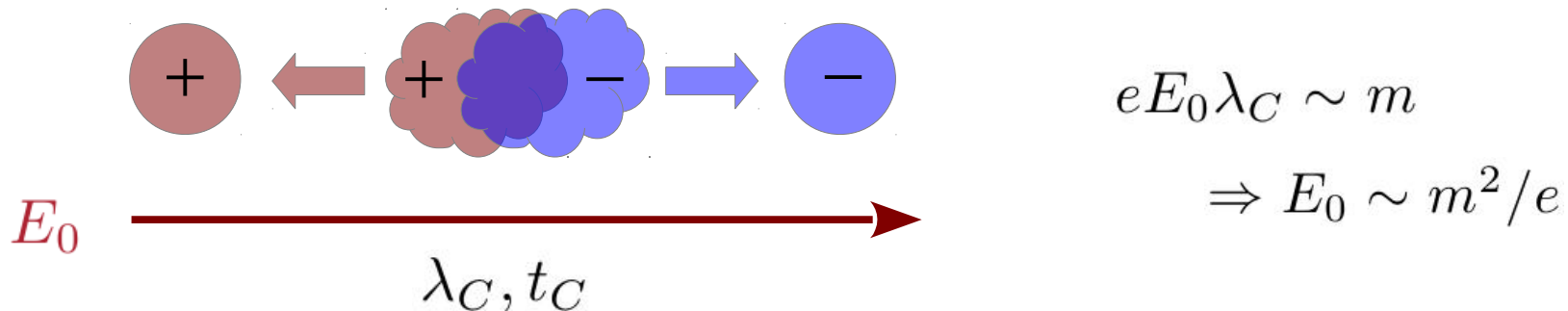
# Motivation: Schwinger effect

- QED vacuum is **unstable** in the presence of external fields

**vacuum**: no particles

**vacuum + electric field**: unstable vacuum (particle creation)

- electron-positron pair creation  $\longrightarrow$  **delocalization** of charges



- analytic solution for **vacuum decay rate** in a static electric field

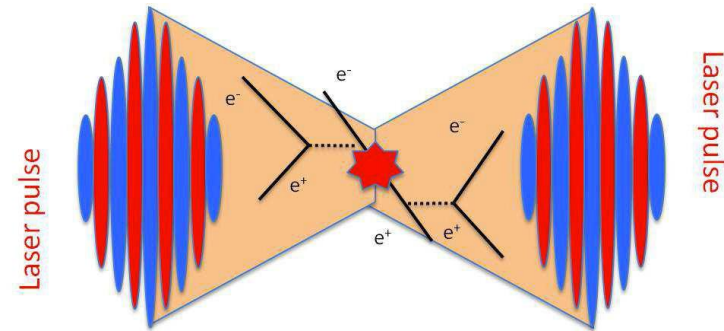
$$\mathcal{P}[vac] = \frac{(eE_0)^2}{4\pi^3} \sum_{n=1}^{\infty} \frac{1}{n^2} \exp\left(-\frac{n\pi m^2}{eE_0}\right) \quad \text{[Schwinger, PR 82 (1951)]}$$

# Motivation: Schwinger effect

- experimental prospects (all optical): **colliding laser pulses**

\* Extreme Light Infrastructure (optical)

\* European XFEL (X-ray)



[Bulanov et al.]

## **space-time dependent electromagnetic fields**

- effect of temporal/spatial structure: **momentum spectrum...**
- effect of electromagnetic fields: **instabilities...**
- effect of created particles (backreaction): **QED avalanches...**

# Outline

- real-time gauge theory with fermions
- Schwinger effect and plasma oscillations
- pulsed fields with sub-cycle structure
- self-bunching in space-time pulses
- a model for QCD dynamics & string breaking
- summary
- open questions & ongoing projects

# Quantum electrodynamics

- theory of the interaction of **matter** (electrons) with **light** (photons)

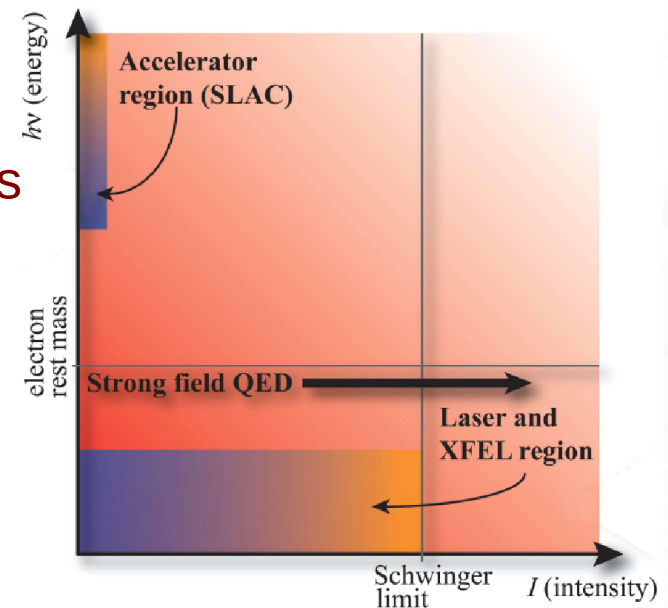
$$\mathcal{L} = \bar{\psi}(i\cancel{\partial} - m)\psi - \frac{1}{4}F^{\mu\nu}F_{\mu\nu} - g\bar{\psi}A\psi$$

- perturbative QED**

low intensity – high energy: **accelerator physics**

- strong field QED**

high intensity – low energy: **laser physics**



[Marklund, Lundin]

# Non-equilibrium quantum field theory

time evolution: **initial value problem** in QFT

$$Z = \int \mathcal{D}\varphi e^{iS[\varphi]}$$

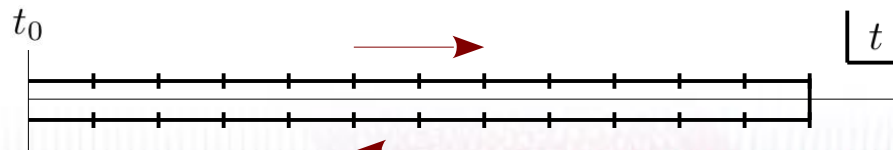
no probability measure  
(sign problem!)

- why not use perturbation theory? **SECULARITY**
- non-secular **approximation** of the generating functional?!

$$Z[J, \eta, \bar{\eta}] = \text{Tr} \left[ \hat{\rho}(t_0) T_C \exp \left( i \int_C J^\mu A_\mu + \bar{\psi} \eta + \bar{\eta} \psi \right) \right]$$

density matrix at **initial time**

time-ordering on the **Schwinger-Keldysh contour**



# Outline of the derivation

- **functional integral** representation:

$$Z = \int [\mathcal{D}A] \int [\mathcal{D}\psi \mathcal{D}\bar{\psi}] \rho_0(\psi, \bar{\psi}, A) \exp \left( i \int_{\mathcal{C}} \mathcal{L}_G[A] + \mathcal{L}_F[\psi, \bar{\psi}, A] \right)$$

- **integrate out** fermions (non-linear effective theory):

$$Z = \int [\mathcal{D}A] \rho_G(A) \exp \left( \text{Tr}_{\mathcal{C}} \log \Delta[A]^{-1} + i \int_{\mathcal{C}} \mathcal{L}_G[A] \right)$$

- **Keldysh rotation**  $A^{\pm} = \bar{A} \pm \tilde{A}/2$  and expansion in  $\tilde{A}$ :

$$\text{Tr}_{\mathcal{C}} \log \Delta[A]^{-1} = \text{Tr}_{\mathcal{C}} \log \Delta[\bar{A}]^{-1} + \frac{g}{2} \text{Tr}_{\mathcal{C}} \left\{ \Delta[\bar{A}] \text{sig}_{\mathcal{C}} \tilde{A} \right\} + \mathcal{O}(\tilde{A}^2)$$



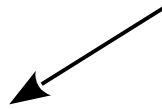
**That's the approximation!**



# Outline of the derivation

- classical-statistical approximation of the **generating functional**:

$$Z = \int [\mathcal{D}\bar{A}][\mathcal{D}\tilde{A}] \rho_G(A) \exp \left( i \int_{t_0}^{t_f} \int_{\mathbf{x}} \tilde{A}^\nu \left\{ \partial^\mu \bar{F}_{\mu\nu} + \frac{g}{2} \text{tr}[\Delta_K \gamma_\nu] \right\} \right)$$



sampling over **initial conditions**



$$\Delta_K(x, y) \equiv \langle [\psi(x), \bar{\psi}(y)] \rangle_{\bar{A}}$$

classical **equations of motion**

$$(i\cancel{\partial}_x - e\vec{A}(x) - m)\Delta_K(x, y) = 0$$

$$\partial^\mu \bar{F}_{\mu\nu}(x) = -\frac{g}{2} \text{tr}[\Delta_K(x, x)\gamma_\nu]$$

- observables** in classical-statistical approximation:

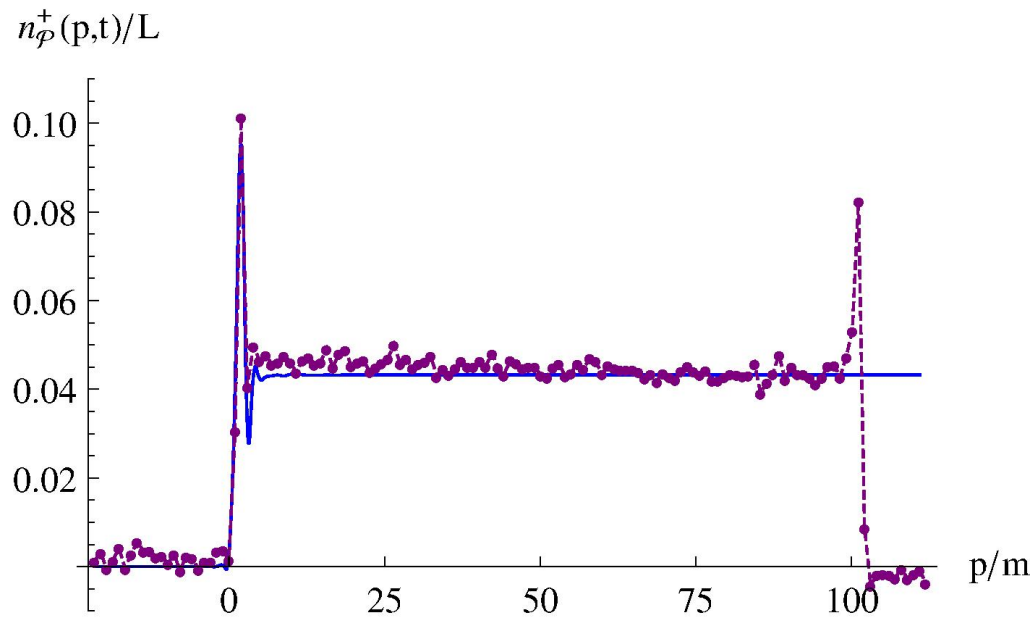
$$\langle O \rangle_{\text{cl}} = \int [\mathcal{D}\bar{A}][\mathcal{D}\Pi_0] \rho_W[\bar{A}_0, \Pi_0] O[\bar{A}] \delta[\text{E.o.M.}]$$

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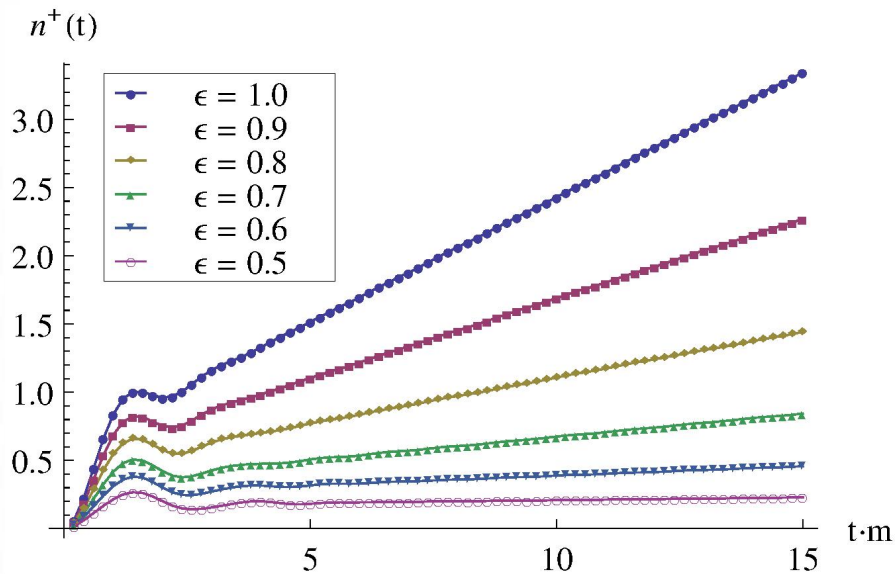
# Schwinger formula on the lattice

static electric field **without backreaction** in QED (1+1)



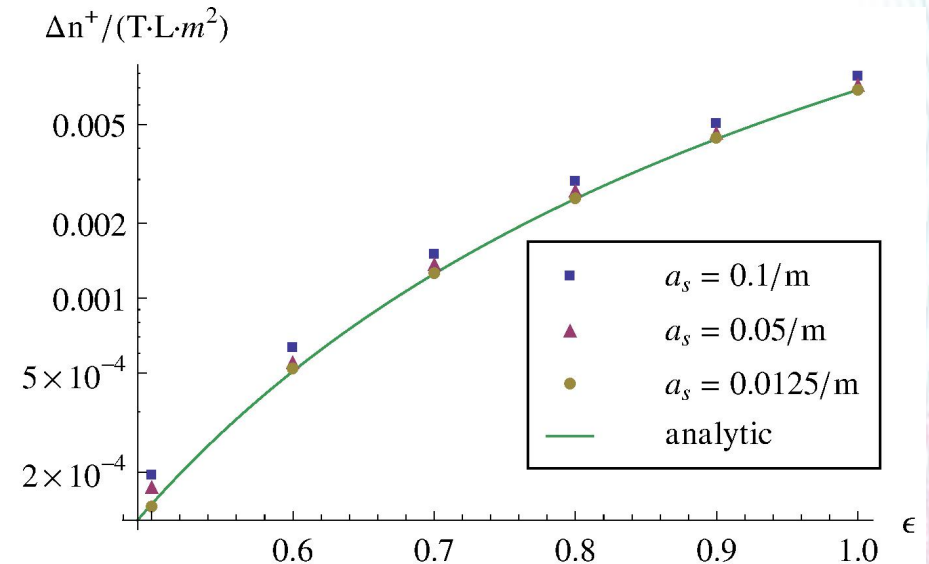
# Schwinger formula on the lattice

static electric field **without backreaction** in QED (1+1)



↑  
transient effect

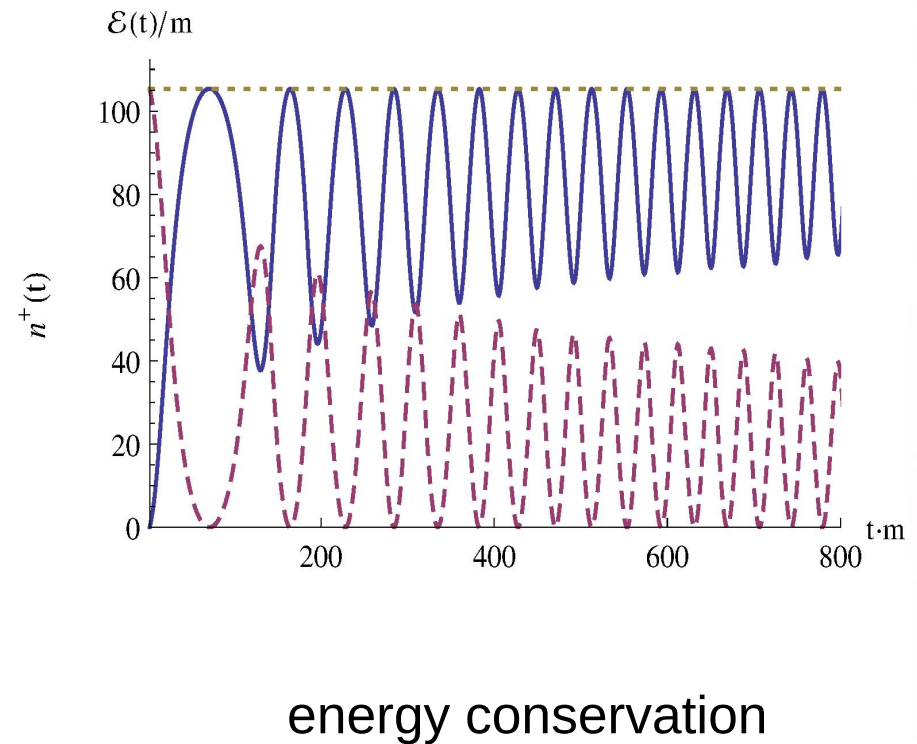
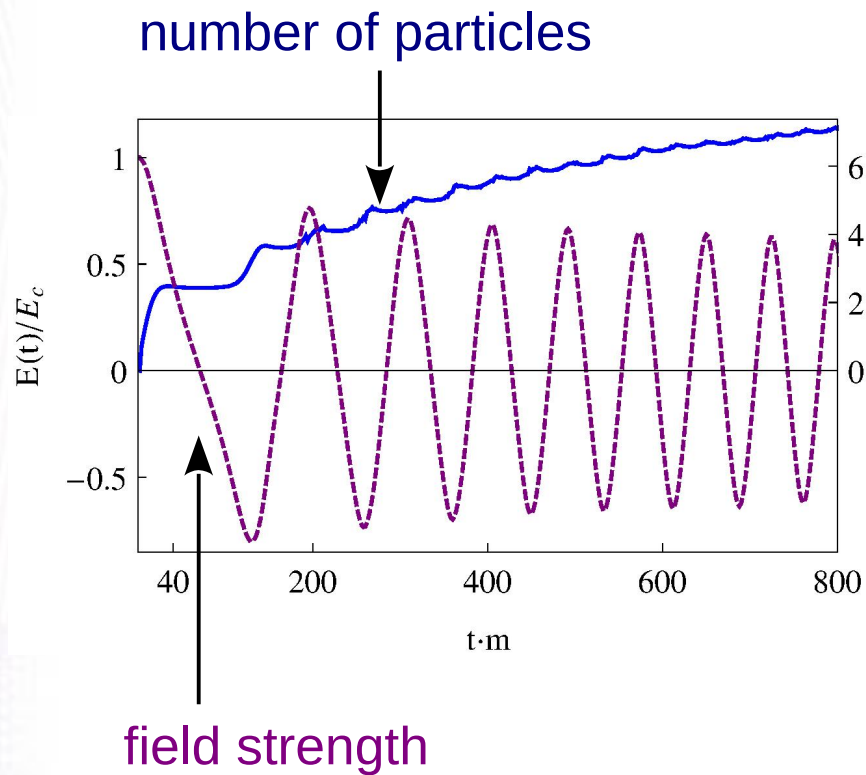
↑  
linear growth



$$\frac{\Delta n^+}{T L m^2} = \frac{\epsilon}{2\pi} \exp\left(-\frac{\pi}{\epsilon}\right)$$

# Plasma oscillations

static electric field **incl. backreaction** in QED (1+1)



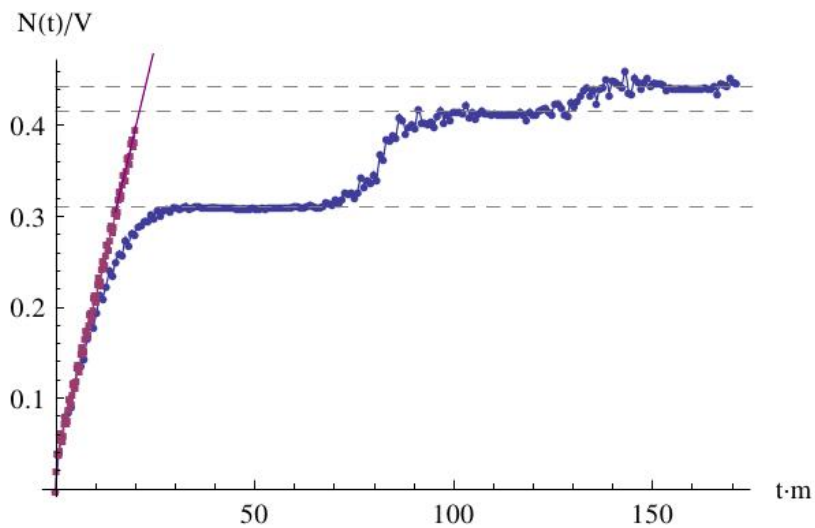
# Plasma oscillations

static electric field **incl. backreaction** in QED (1+1)

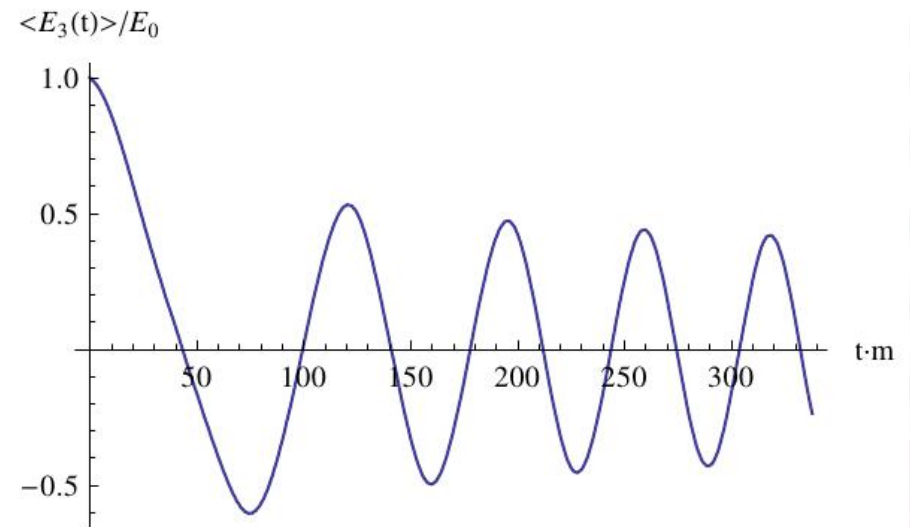


# Plasma oscillations

static electric field **incl. backreaction** in QED (3+1)



number of particles



field strength

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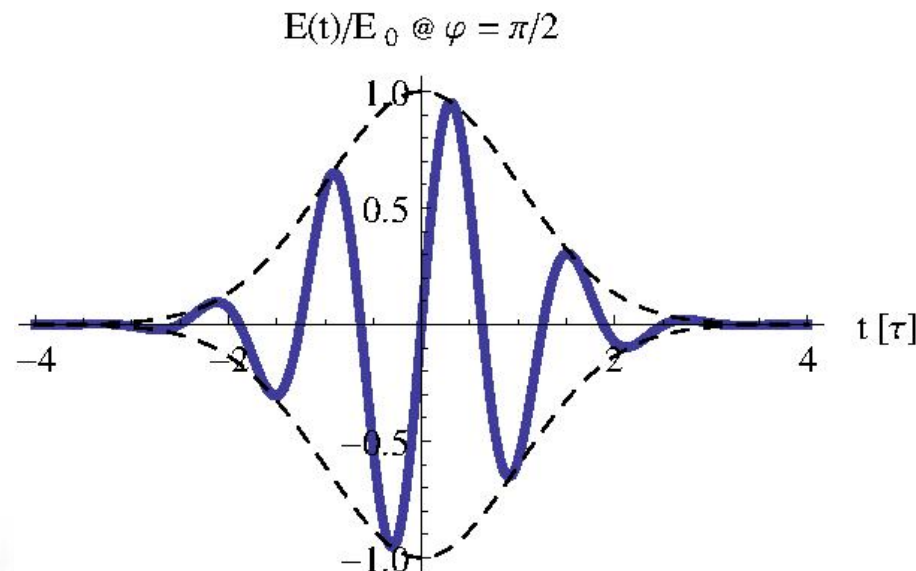
# Pulsed field with sub-cycle structure

- Schwinger effect in **colliding laser pulses**  $\longrightarrow$  simple model:  
two **counter-propagating** laser pulses: standing wave  
in the **focus of optical laser systems**: t-dependent electric field

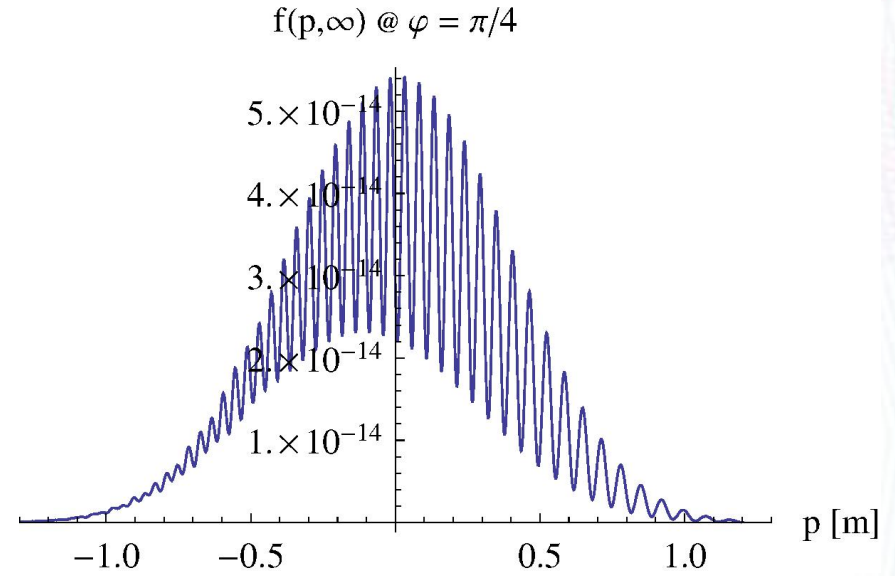
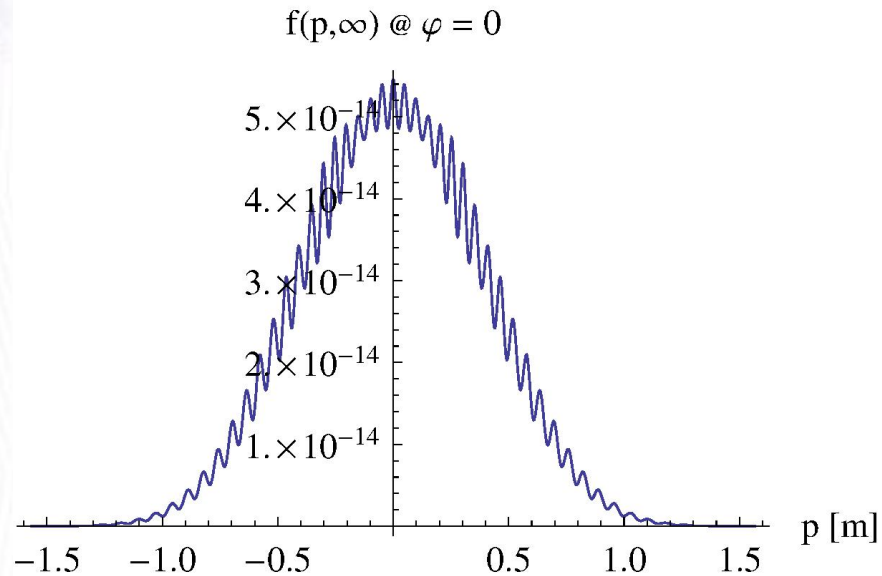
$$E(t) = E_0 \cos(\omega t - \varphi) \exp(-t^2/2\tau^2)$$

$$\sigma = \omega\tau$$

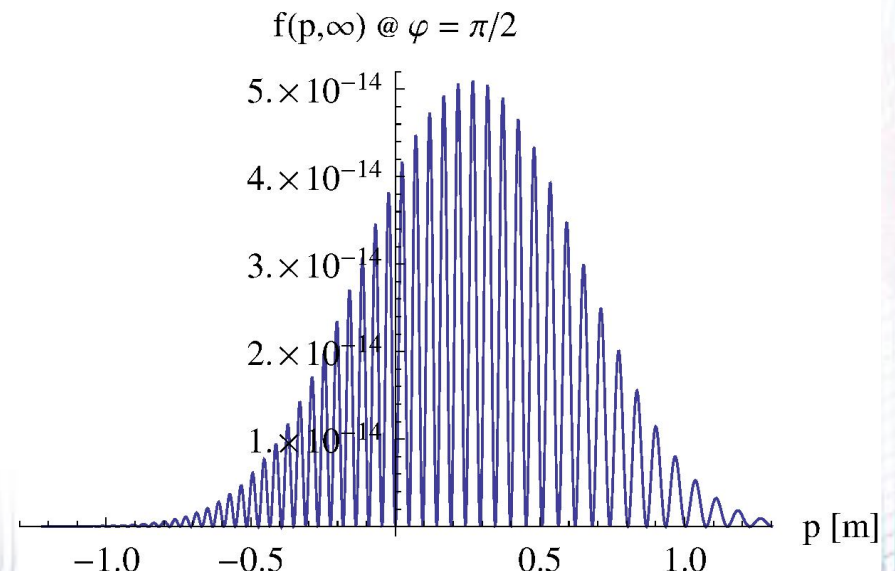
number of cycles



# Pulsed field with sub-cycle structure

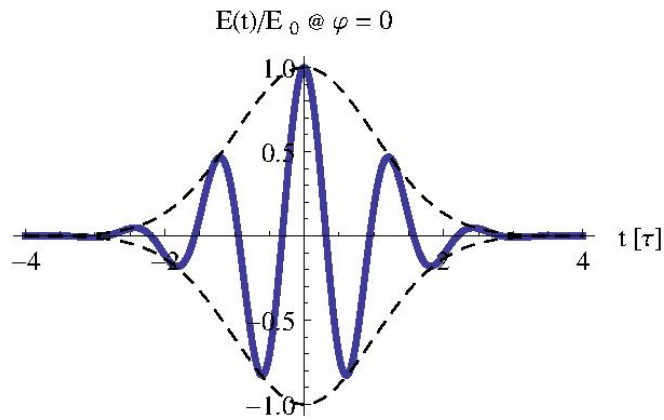


- extremely sensitive to **CEP**  
→ resonance phenomenon
- matterless **double-slit** in time  
→ quantum interference
- in general: **temporal variations**  
→ distinctive signatures



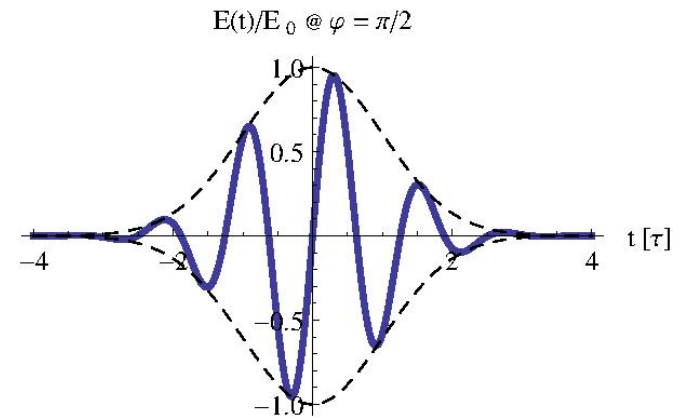
# Matterless double slit in time

- 'attosecond double slit experiment' in **photoionization**  
[Lindner et al., PRL 95 (2005)]
- here: interference of **temporally separated pair creation events**



**one** dominant production event  
=  
**single slit**

weak interference pattern



**two** equal production events  
=  
**double slit**

maximum interference pattern

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# Bunching in space-time pulse

single electric pulse in **space** and **time** in QED (1+1)

$$E(x, t) = E_0 \operatorname{sech}^2(\omega t) \exp(-x^2/2\lambda^2)$$



fermion density

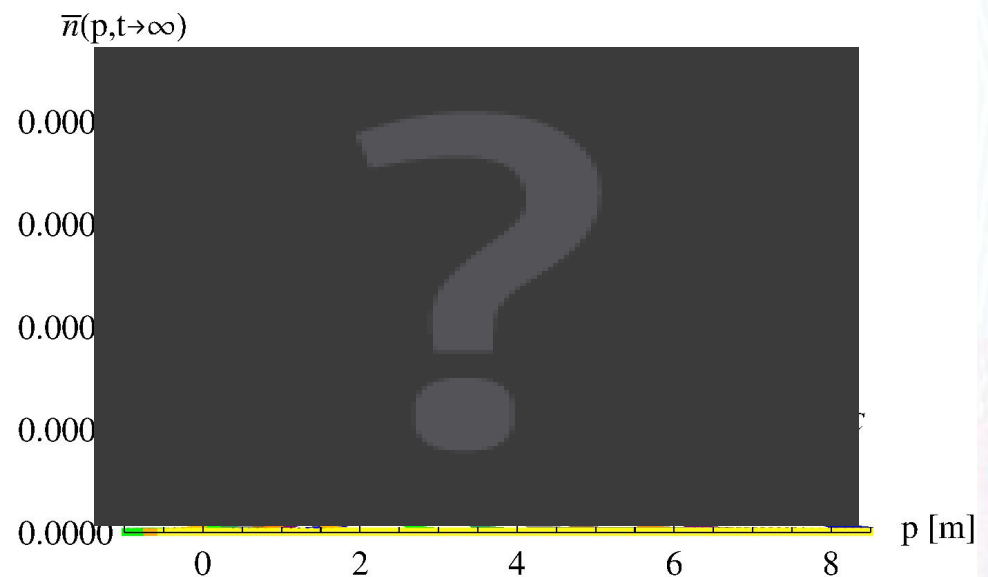
charge density

electric field

# Self-bunching in space-time pulse

single electric pulse in **space** and **time** in QED (1+1)

- **scaling** as function of  $\lambda$   
→  $\bar{n}(p, t) = n(p, t)/\lambda$
- **self-bunching** of  $\bar{n}(p, t)$   
→ **higher** and **narrower**
- **termination**  
→ sharp drop for small  $\lambda$
- **interplay**: temporal/spatial scales

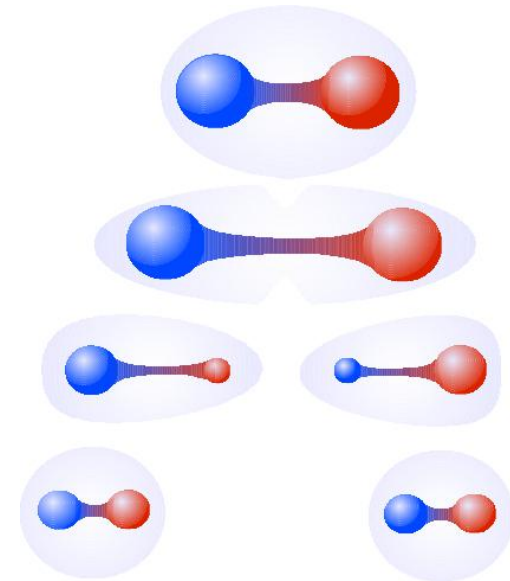
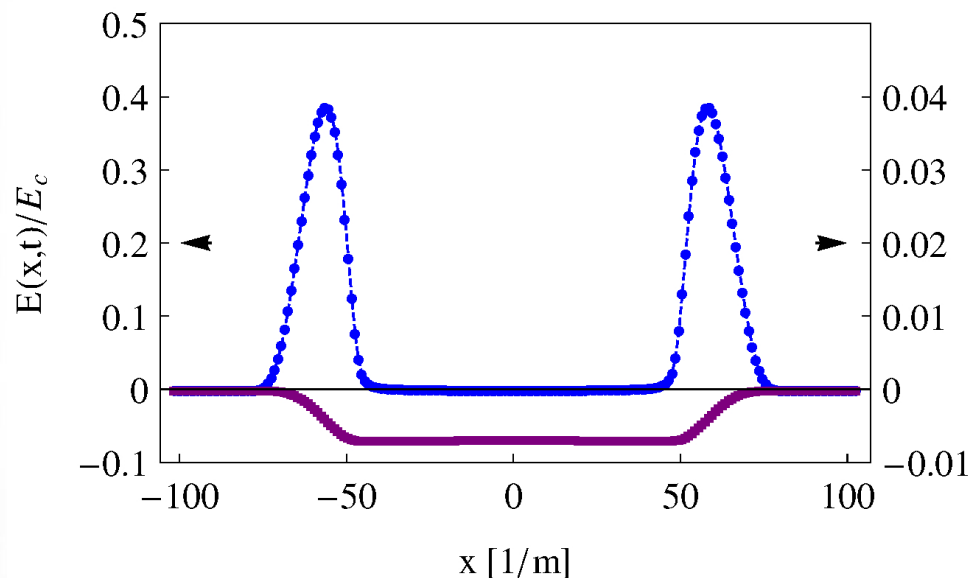


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# The string breaking analogue

- fermion bunches act as **capacitor**
- 1+1 dimensional geometry: **Coulomb potential = linear potential**  
 cf. **QCD string breaking**: linear potential due to strong interaction



**Can we learn something about the dynamics of string breaking?**



# Dynamics of string breaking

two **static charges** separated by distance  $d_C$



# Dynamics of string breaking

two **static charges** separated by distance  $d_C$

- two-stage process (different scales)
  - **creation** on top of each other
  - **separation** of charges

- Naïve estimate for **critical distance**

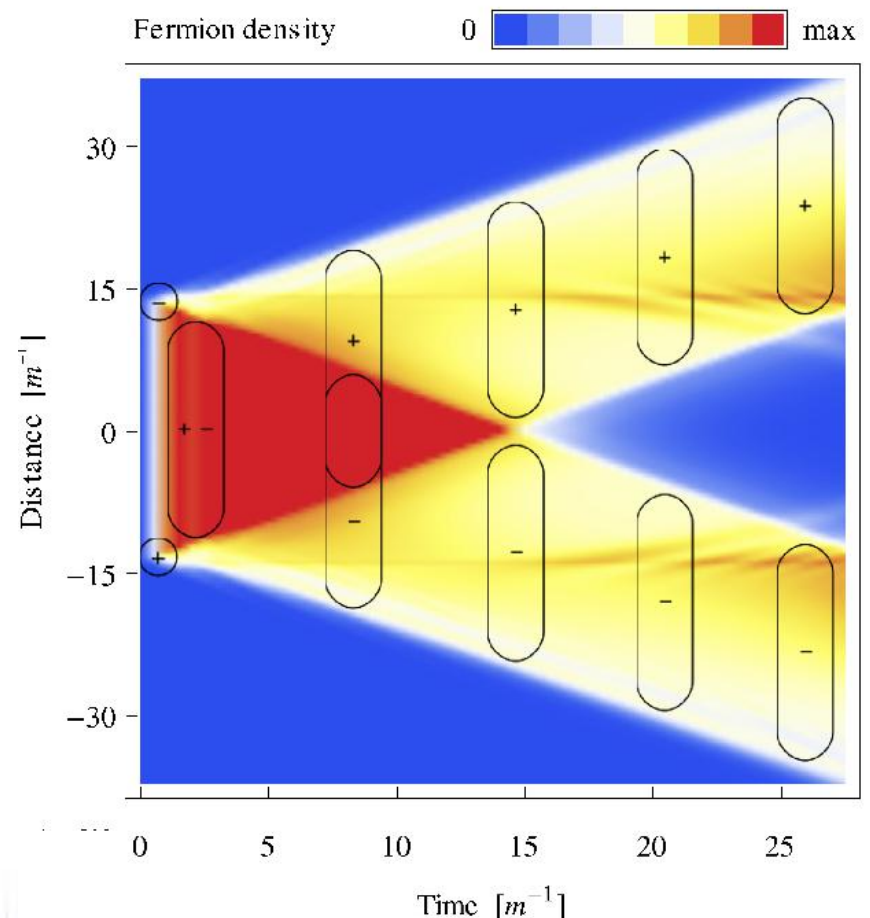
$$V_{\text{str}}[d_C] = 2m$$

↓ **modified**

$$V_{\text{str}}[d_C] = 2m + W[d_C]$$

- very substantial **work contribution**

$$W[d_C] > 2m$$



# Dynamics of string breaking

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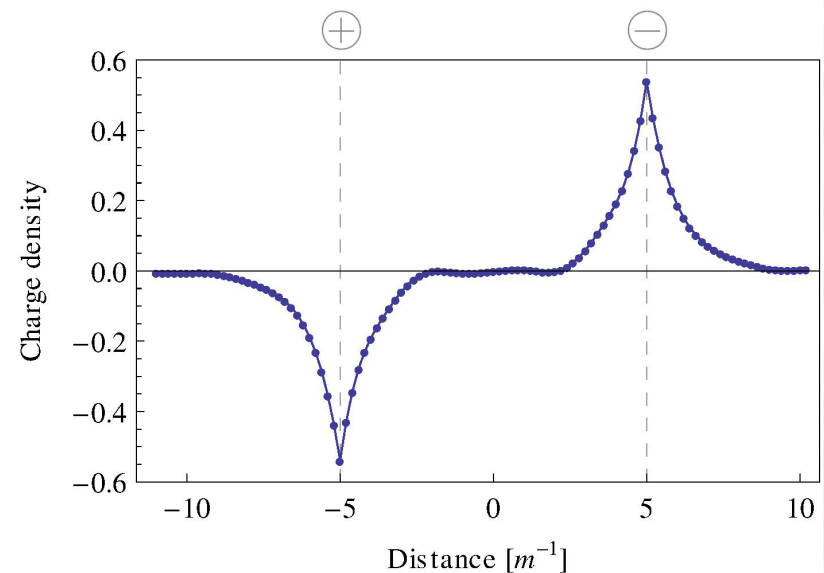
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**asymptotic screening**

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# summary (take-home lessons)



(a)

[together with: C. Kohlfürst , R. Alkofer]

# Enhancement & pulse optimization

- **dynamically assisted** Schwinger mechanism

[Schutzhold, Gies, Dunne, PRL 101 (2008)]

- **time-domain multiple slit interference**

[Akkermans, Dunne, PRL 108 (2012)]

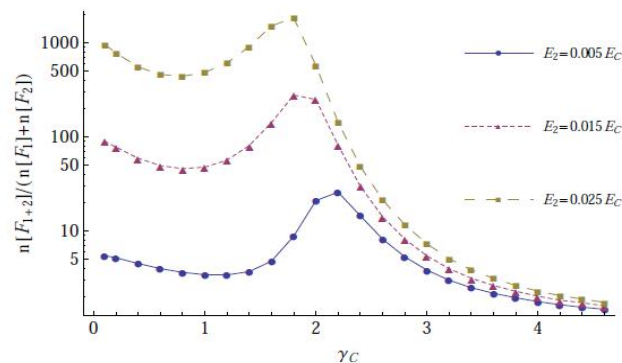


FIG. 1: Enhancement of the particle density in the dynamically assisted Schwinger mechanism. The parameters of the adiabatic pulse are given by  $E_1 = 0.1E_c$  and  $\omega_1 \sim m/100$ . The different curves correspond to different values of  $E_2$  and we change  $\gamma_c$  or, equivalently,  $\omega_2$ .

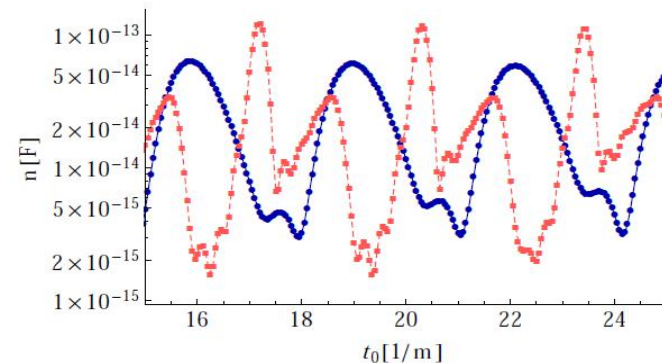


FIG. 2: Particle density for of a comb of 10 single pulses with parameter  $|E_i| = 0.02E_c$ ,  $\omega_i = m/6$  for the equal-sign configuration (solid) and the alternating-sign configuration (dashed). The particle number changes quasi-periodically by orders of magnitude as function of the inter-pulse time lag  $t_0$ .

- **optimal control theory:** systematic shaping under constraints

[Kohlfurst, Mitter, von Winckel, FH, Alkofer, PRD 88 (2013)]

- **current investigations:** pulse optimization & inverse problem

(b)

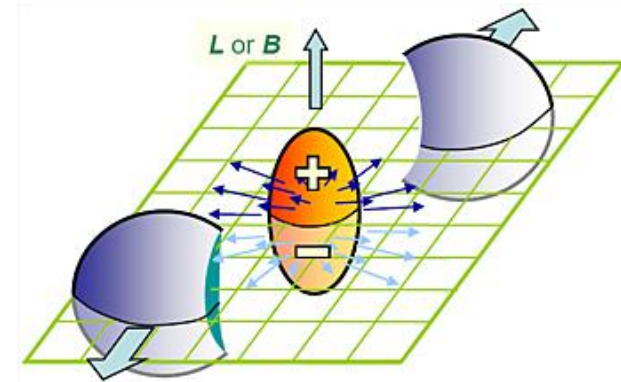
[together with: N. Müller , L. Palhares, J. Berges]

# Chiral magnetic effect (in QED)

- possible explanation of **charge asymmetry in HIC** (STAR '08)

topol. charge + axial anomaly + magnetic field  
=  
**electric current in the perp. direction**

[Kharzeev, McLerran, Warringa, Nucl. Phys. A (2008)]

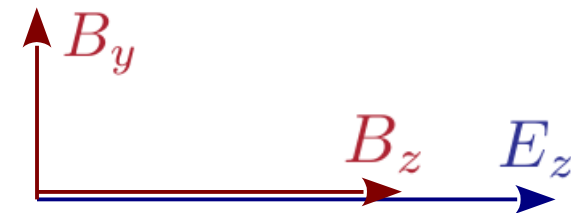


- current investigations: **chiral magnetic effect in QED**

→ topological config.:  $B_z E_z$

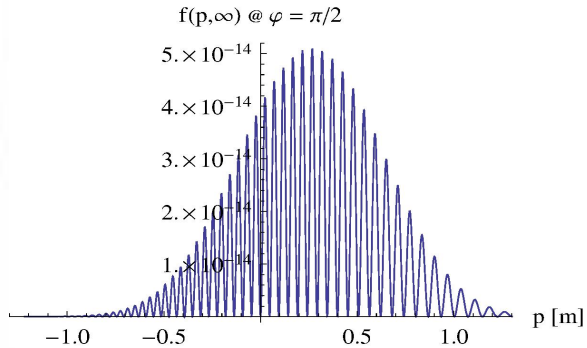
→ magnetic field:  $B_y$

→ 'proposal': **4 ultrahigh-intensity lasers**

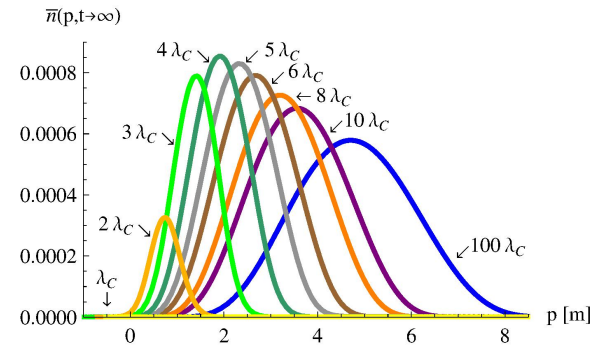


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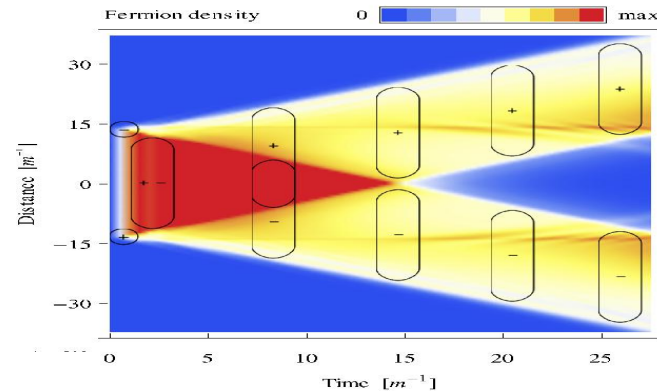
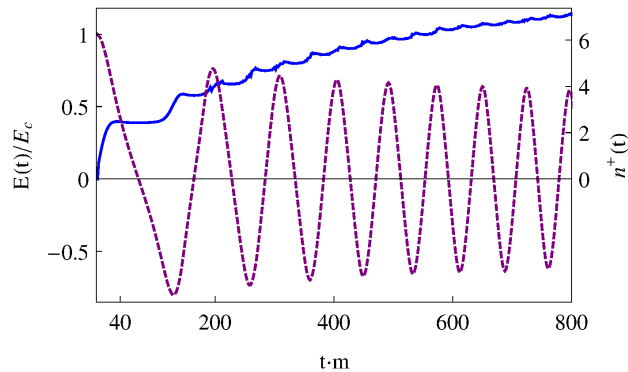
temporal variations



spatial and temporal variations



backreaction and collective phenomena



Thank you!